

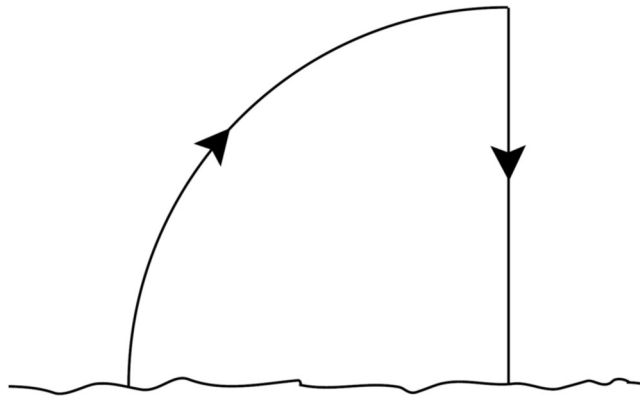
Lecture Notes

(Projectile Motion)

Intro:

- the previous chapters have considered motion mainly in a straight line; this is called rectilinear motion (Latin *rectus* = 'straight' and *linea* = 'line')
- this chapter will be looking at motion in two dimensions, that is, curvilinear motion
- projectiles from cannons, a shotput, throwing a baseball, motorcyclists jumping rows of cars; and ballet dancers all involve curvilinear motion
- until the time of Galileo, the motion of a projectile was based on the teachings of Greek philosopher Aristotle

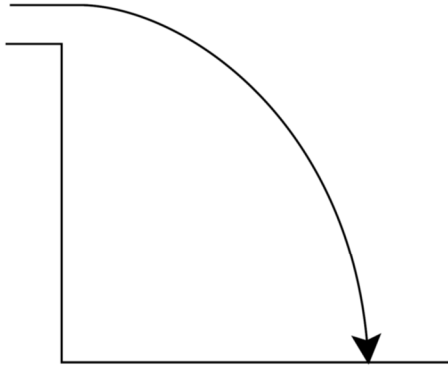
Until the 1600s, people thought that projectile motion was more like this.



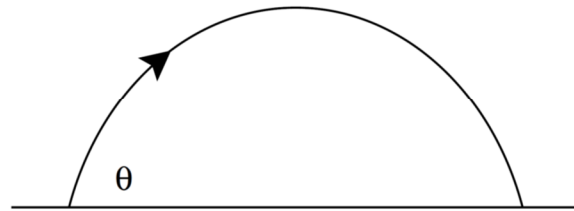
- it wasn't until 1638 that the trajectory of a projectile could be described mathematically
- Galileo's description proved to be correct and has been the basis of mechanics since

Projectile Motion:

- good examples of projectiles are a rock thrown straight out from the top of a cliff and a ball thrown across a field



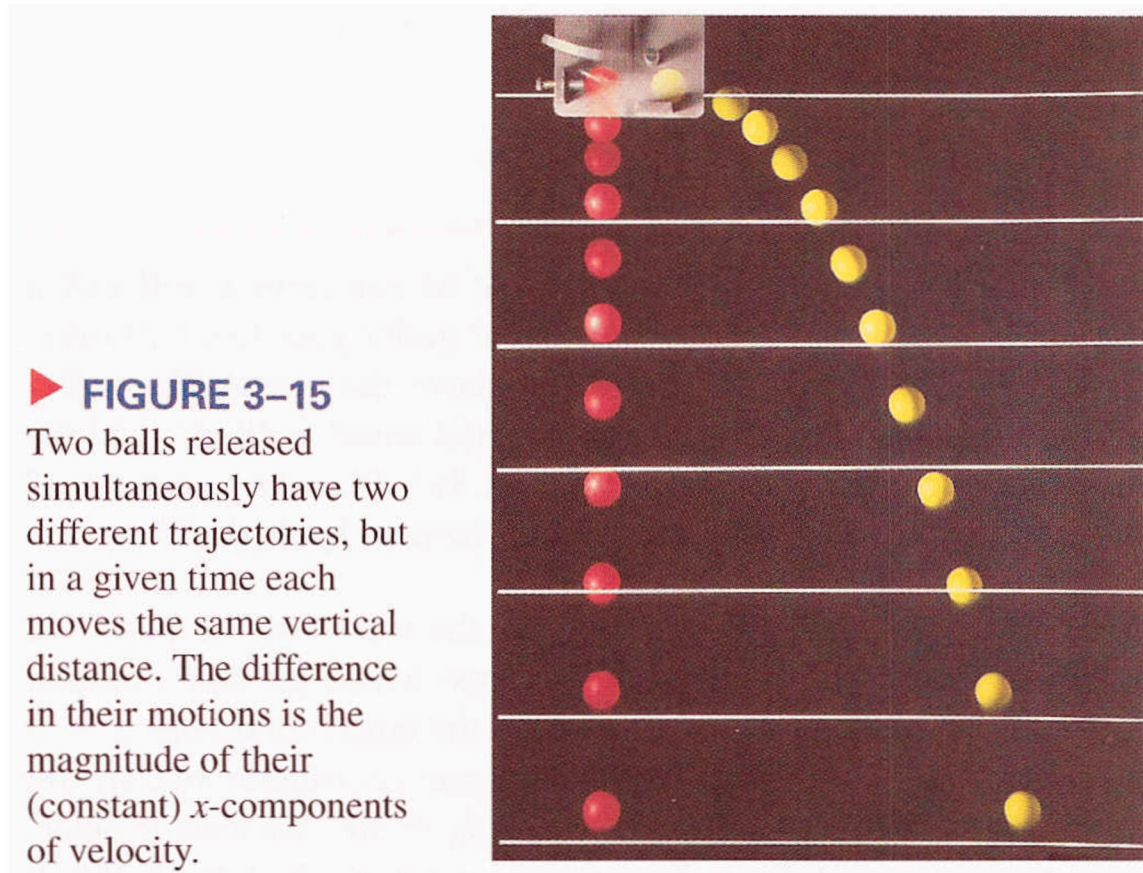
Horizontal projection
— a rock thrown off
a cliff



Angled projection — a
cricket ball thrown
across a field

- the word projectile comes from the Latin jacere meaning ‘to throw’ and pro meaning ‘forward’
- projectile motion can be separated into two components; a vertical (up and down) motion and a horizontal motion
- the vertical motion is the same as discussed earlier, the ball is under the influence of gravity and accelerates at 9.8 m/s^2 directed downward (the negative direction)
- in the horizontal direction, there are no net forces acting on the object so the velocity is constant
- in all cases we are assuming air resistance is negligible
- the path of a moving object is called its trajectory (Latin trajetus means ‘crossing’ or ‘passage’)
- a projectile is an object that once given an initial thrust, it moves through the air only under the force of gravity

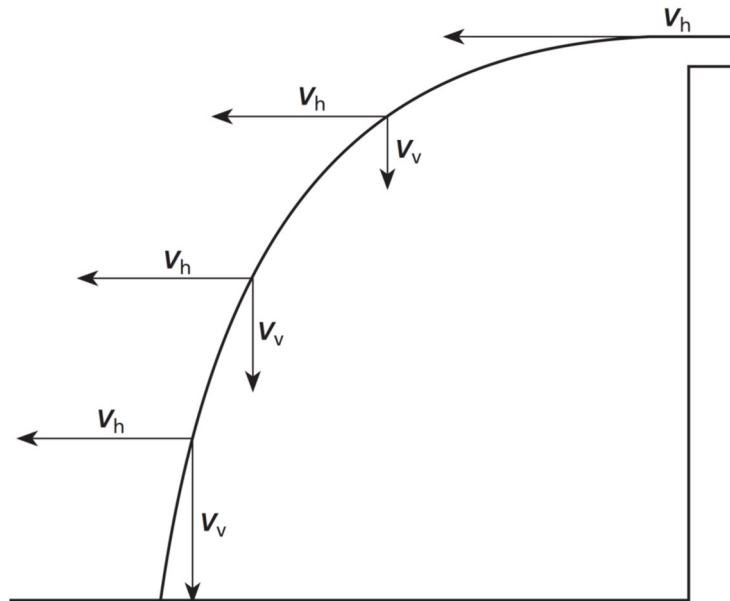
Independence of Motion in Two Dimensions:



- take a look at the example above; we have two golf balls photographed with a strobe light that flashed 30 times per second
- the ball on the right was given a horizontal velocity; the ball on the left was dropped; you can see that the balls are accelerated downward by the force of gravity
- note that the vertical positions of the two balls are the same at each flash of the strobe light; the horizontal positions differ over time
- the constant horizontal velocity and vertical acceleration produces a trajectory that has the shape of a curve called a parabola

Projectiles Launched Horizontally:

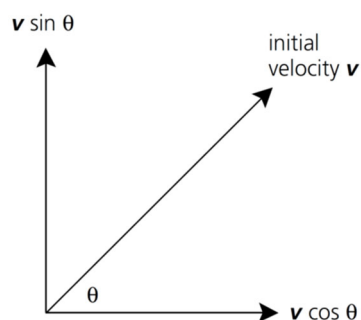
- projectiles launched horizontally have no initial vertical velocity



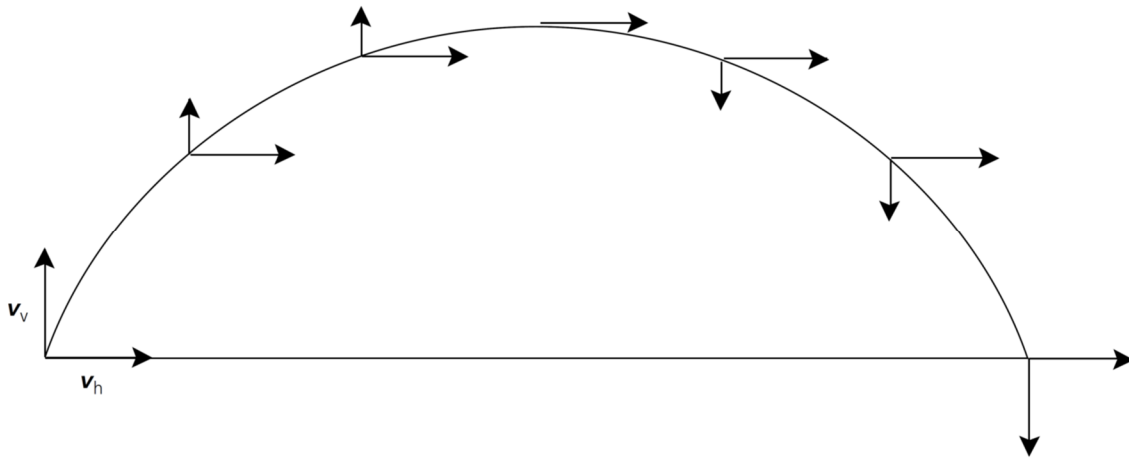
- as a result, the vertical motion is identical to that of a dropped object
- the downward velocity increases due to the acceleration due to gravity

Projectiles Launched Vertically:

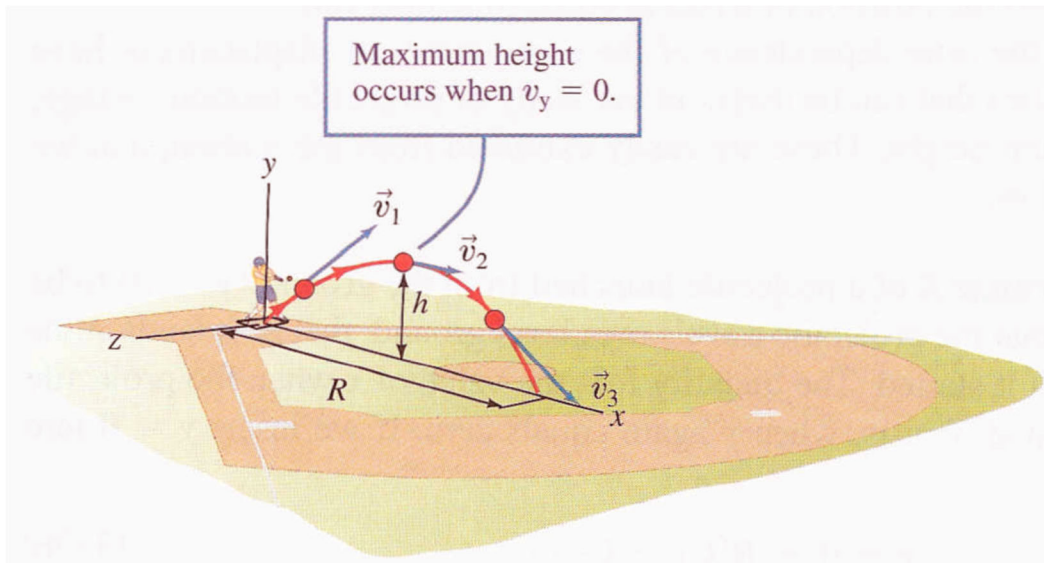
- not all objects are thrown in a horizontal direction; cannonballs, footballs for example, are often projected upward at an angle
- to study projectile motion, we let θ be the angle at which the object is thrown relative to the horizontal; this is called the elevation angle



- when a projectile is launched at an angle, the initial velocity has a vertical component as well as a horizontal component



- if an object is launched upward, it rises with slowing speed, reaches the top of its path (zero vertical velocity), and descends with increasing speed
- at each point in the vertical direction, the velocity of the object, as it is moving up, has the same magnitude as when it is moving down; their directions, however, are opposite
- the impact velocity will have the same magnitude as the launch velocity, but be directed in a general downward direction not upward as at launch
- there are three quantities associated with trajectory; 1) maximum height, 2) range, and 3) flight time
- the range is the horizontal distance the projectile travels to reach the same height from which it started
- maximum height is the height of the projectile when the vertical velocity is zero and the projectile has only its horizontal velocity component

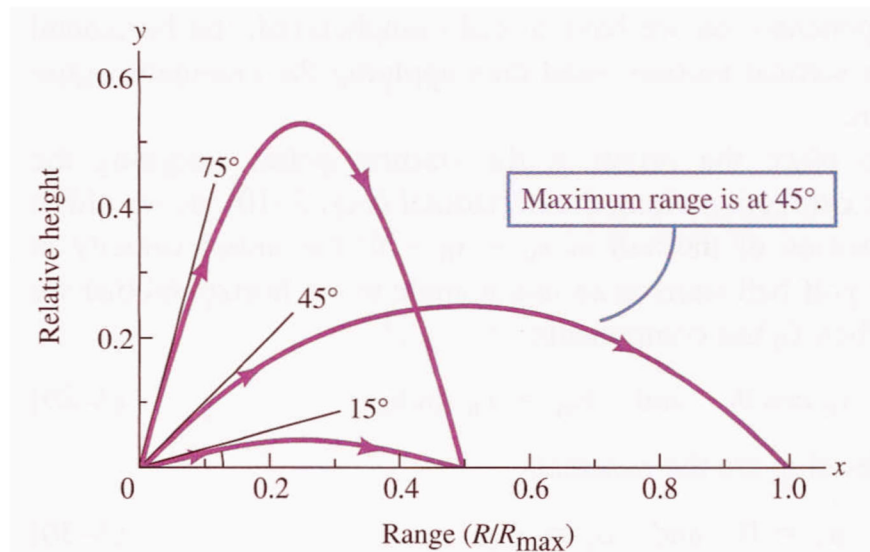


- flight time is another term used with projectile motion; it refers to the amount of time the projectile is in the air
- at exactly halfway through its trajectory the projectile will reach maximum height; the time it takes to reach max height is flight time/2

Maximum Range:

- it was the invention of the cannon in the late 1400s that created a new form of warfare; war at sea using cannons became more common and defense using medieval castles became obsolete
- medieval mechanics also became obsolete. Until then, the motion of a projectile was only of philosophical interest because they all thought they knew how projectiles moved
- after all, Aristotle described the motion over 1000 years earlier and no one was prepared to challenge his theories
- the theories weren't challenged until they had to be tested in warfare and were found wanting

- aiming was very much a hit-or-miss affair; there was no way of determining the trajectory or even the angle of launch in advance
- it wasn't until self-taught engineer Niccolo Fontana published the results of his experiments in 1546 that gunners realized a 45° angle of elevation would give the maximum range



Air Resistance:

- air resistance has been left out of our discussions up to this point, but in the real world it plays a significant role in projectile motion
- for some streamlined, heavy objects, air resistance is minimal; but for other objects, it plays a large factor in the trajectory of a projectile
- the speed of an object also play a role in air resistance; the greater the speed of an object the greater the air resistance

